

Efficient readout of micromechanical resonator arrays in ambient conditions

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(Dated: June 6, 2009)

We present a method for efficient spectral readout of mechanical resonator arrays in dissipative environments. Magnetomotive drive and detection is used to drive double clamped resonators in the nonlinear regime. Resonators with almost identical resonance frequencies can be tracked individually by sweeping the drive power. Measurements are performed at room temperature and atmospheric pressure. These conditions enable application in high throughput resonant sensor arrays.

PACS numbers: + 85.80.Jm, 05.45.-a

Micro- and nanometer scale mechanical resonators are widely considered as mass and force sensors. Ad- or desorption of molecules by the resonator are detected as slight changes in resonance frequency. Several methods exist to measure the resonance frequency of a single resonator [1, 2, 3, 4]. Small arrays of static mechanical sensors be scanned optically [5] or the reflection of the array as a whole may be analyzed [6]. Spectral readout of small-scale resonant arrays has been reported in vacuum [7]. In this letter we present an efficient method to readout resonators with closely spaced resonance frequencies in dissipative environments. We show that the number of resonant sensors which can be operated in a given bandwidth is not limited by the Q factor. Using a magnetomotive setup we can discriminate mechanical resonators with almost identical frequencies in ambient conditions.

To track two individual resonators with quality factor Q in a frequency spectrum, their resonance frequencies f_i should be separated by at least $\Delta f = f_i/Q$. Simultaneous operation of n resonators requires a minimum bandwidth on the order of $\Delta f = f_1(1 + 1/Q)^n$. Here f_1 is the resonance frequency of the slowest resonator. In vacuum, the Q -factor of a mechanical resonator can be of the order 10^4 [7], and readout of large arrays of resonators should be feasible. At atmospheric pressure however, Q -factors usually drop below 10^2 because of viscous drag [8]. This limits the number of resonators within a practical bandwidth to a few hundred at most. Large-scale arrays therefore require either multiple detectors or separated drive circuits, and the complexity of such systems rapidly increases with the number of resonators.

To address this problem, we propose to readout arrays of resonators with closely spaced center frequencies by sweeping the drive power from low to high values at constant frequency. Once the nonlinear regime is accessed, individual resonators are marked by instantaneous transitions in the phase and amplitude response. When each nonlinear resonator is used as a sensing element [9], the locations of these characteristic amplitudes

are affected by ad- or desorption induced mass or stress change to the concerning resonator. We conduct experiments on arrays of double clamped resonators at room temperature and atmospheric pressure. We experimentally show that in a 2-D array of 6 resonators with closely spaced resonance frequencies, individual resonators can be discriminated using a single drive and detector unit. Calculations confirm the experimental findings.

Arrays of double clamped mechanical resonators are fabricated out of 100 nm thick low-pressure chemical vapor deposited (LPCVD) silicon nitride by electron beam lithography. All resonators have the same dimensions $200\mu\text{m} \times 15\mu\text{m}$. Slight variations in center frequencies of the resonators are expected as a result of variations in residual stress [10]. Figure 1(a) shows one of the resonators before metallization. A layer of chromium and gold is evaporated on top to enable magnetomotive drive and detection. The resonators share a support on one side, while supports at the other side are separated. This allows the measurement of both the individual and the collective responses.

Figure 1(b) shows the measurement setup schematically. The RF voltage from a network analyzer is converted to a current which drives the resonators (two in series depicted). A magnetic field of 1.9 T is generated by a Halbach array [11] constructed from NdFeB permanent magnets. The resulting voltage is amplified and measured by the network analyzer. This measurement setup can be used at room temperature and atmospheric pressure, in contrast to earlier magnetomotive experiments in vacuum and/or at cryogenic temperatures. As a result

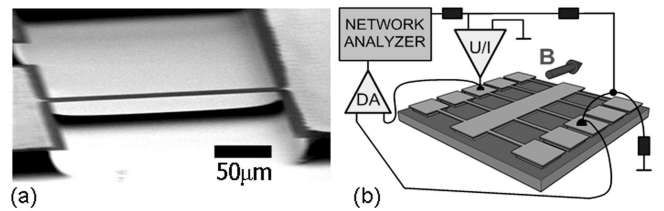


FIG. 1: (a) Scanning electron micrograph of a single resonator. (b) Magnetomotive measurement setup. The current source is formed by the amplifier U/I and the resistor network.

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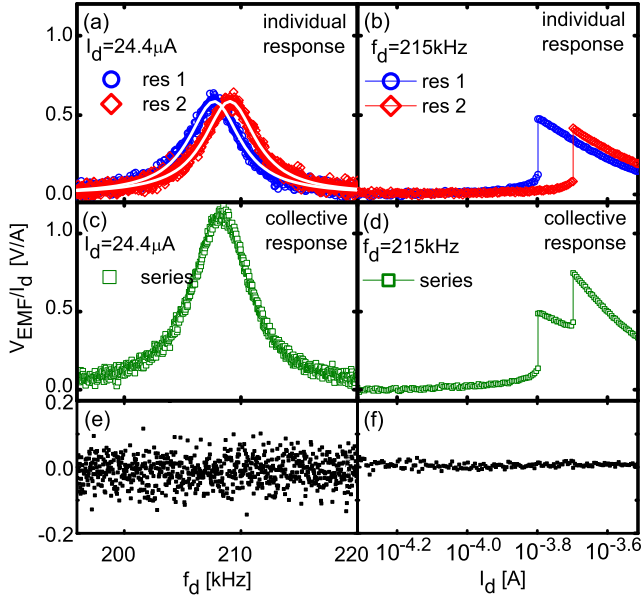


FIG. 2: Magnetomotive measurements in ambient environment. (a) Individual linear frequency response of two resonators with almost identical resonance frequencies. (b) The same resonators driven nonlinear by sweeping drive power at 215kHz. (c,d) Collective response of the resonators connected in series in linear (c) and nonlinear (d) regimes. (e,f) show the difference between the calculated sum of the individual responses and the measured collective response in the linear (e) and the nonlinear (f) regime.

of viscous drag, the Q-factors in our experiments are a factor of 10 to 100 lower than in those experiments.

Figure 2(a) shows the linear response of two resonators with almost identical center frequencies. The voltage drop due to the resistance of the resonator, bond wires etc. has been subtracted. The resonance frequencies and Q-factors are determined by fitting Lorentzian functions (shown in the figure) to the measured data. The resonance frequencies of these devices were 207.72kHz and 209.05kHz, and the Q-factor is 39 for both resonators. The corresponding bandwidth is 5.4kHz, whereas the difference in resonance frequency is 1.3kHz. Now the resonators are connected in series and the collective response is measured. Figure 2(b) shows the result for the same drive conditions as in (a). Discrimination between the two resonators is impossible as the resonator bandwidth is more than four times the difference in center frequency. We now individually drive the same resonators at increasing power at a constant frequency of 215kHz. Fig. 2(d) shows the result: a steep transition in the resonator amplitude marks the characteristic drive amplitude at this frequency. When the collective response is measured at strong driving, as in (d), the two resonators are easily distinguished.

In absence of interaction, the response of multiple resonators is just the sum of the individual responses. To verify this, the difference between the sum of the individ-

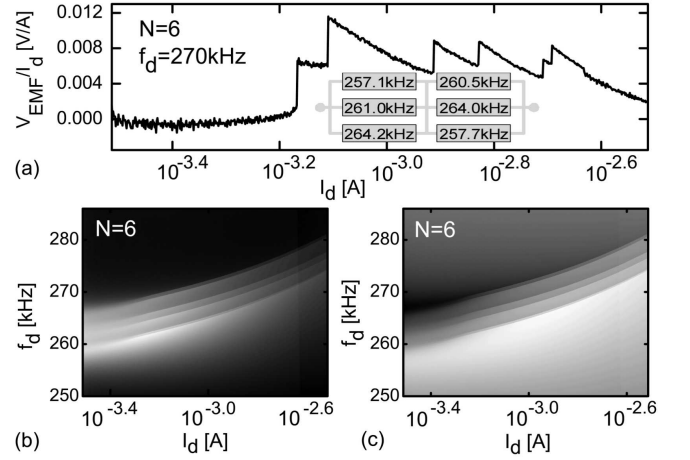


FIG. 3: Measurements on a 2-D array of 6 resonators. (a) Resonator response while sweeping the drive current at $f = 270 \text{ kHz}$. The inset shows the arrangement of the resonators and their linear resonance frequencies. (b) and (c) show amplitude and phase response of the array, driven at different frequencies f_d .

ual responses of (a) and (d) and the collective response in (b) and (e) is plotted in Fig.2 (c) and (f). No amplitude dependency is found, which indicates that the coupling is weak. Note that a high driving power results in a notably lower noise level in the nonlinear driven system [12].

We now turn to a 2-D array of 6 resonators, for which the arrangement and the measured linear resonance frequencies are depicted in the inset of Fig.3(a). In this experiment, the bandwidth of the individual resonators was $5 \pm 0.1 \text{ kHz}$, which corresponds to a Q-factor of approximately 50.

Figure 3(a) shows the nonlinear amplitude response at $f_d = 270 \text{ kHz}$; clearly 6 resonators can be distinguished. In Fig.3(b) and (c), sweeps at fixed drive frequencies ranging from 250kHz to 285kHz are plotted. Six lines marking characteristic jumps in resonator amplitude and phase remain equidistant. Indeed, over the nonlinear regime, the total bandwidth covering the 6 resonators changes by less than 60Hz in this measurement. When sweeping frequency from low to high values at constant drive current (not shown), we found strong coupling between the resonators which causes multiple resonators to collapse simultaneously at high driving power. Strong coupling makes the system useless as an array of independent sensors.

As for the differences in the center frequencies of the resonators, we note that in LPCVD silicon nitride residual stress variations of the order of 10% across a 2' wafer are not unusual [10]. Using this number, the residual stress gradient would be on the order of 100 Pa/ μm . Given the distance between the resonators (at least 300 μm) the difference in residual stress is on the order of 10^4 Pa which results in frequency differences on the order of 100Hz. Similar frequency differences can be obtained by slightly varying the geometry of the resonators

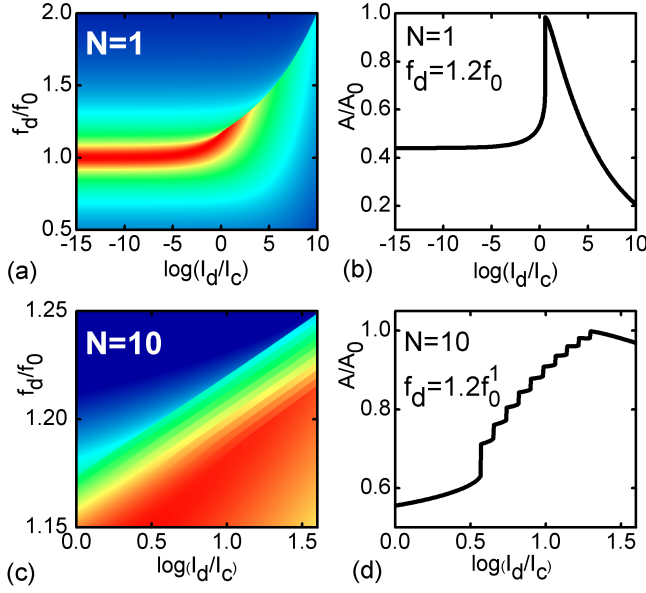


FIG. 4: Calculated amplitude responses. (a) Normalized amplitude response of a single resonator driven at fixed frequency as a function of the normalized drive amplitude f_d/f_0 . (b) Cross section at $f_d/f_0 = 1.2$. (c) and (d) show the amplitude response for ten resonators.

or the thickness of the deposited gold layer.

To corroborate the experimental results, we have calculated the characteristic driving amplitude of a non-linear resonator at a given driving frequency by solving the equation of motion:

$$M\ddot{y} + C\dot{y} + (K_t + K_b)y + K_3y^3 = BLI_d \cos(\omega t), \quad (1)$$

where M is the resonator effective mass, y the beam displacement C the damping constant, and K_t and K_b represent linear stiffness terms due to residual tension and bending rigidity respectively. The nonlinear term K_3 is a result of the elongation of the beam, L is the beam length, B the magnetic field strength and I_d the driving current.

For the beams in Fig.2, the average residual tension $T_0 = 74\mu\text{N}$ is found by comparing the calculated stress-free resonance frequency to the measured resonance frequency [13]. We calculated that $K_t/K_b \approx 85$, which indicates that the bending rigidity of the resonators is insignificant and the linear resonance frequency is merely determined by M and K_t . The magnetomotive voltage

generated by the string-like linear resonator at resonance equals:

$$V_{EMF} = \frac{4}{\pi^4} \frac{\omega_1 I_d B^2 Q L^3}{T_0}. \quad (2)$$

With the experimental values $B = 1.9$ T, and $Q = 39$, and $L = 200$ μm , the transduction at resonance equals $V_{EMF}/I_d = 0.8$ V/A.

Instead of the frequency-dependent resonator amplitude while varying the drive amplitude at constant frequency f_d to mimic the experimental situation. Thus, out of two stable states, the resonator always vibrates at the lowest amplitude. Figure 4(a) shows the calculated response for a resonator similar to ones used in the experiments. The frequency axis is normalized to the linear resonance frequency f_0 , and traces for the normalized drive frequencies f_d/f_0 from 0.5 to 2.0 are combined in (a). Red regions correspond to a high amplitude. The trace for $f_d/f_0 = 1.2$ is shown in Fig.4(b). Sweeping parallel to the horizontal axis, locations with multi-valued resonator amplitudes are accessible at large drive amplitudes, when $f_d > f_0$. Figure 4(c) shows the simulated response of an array of 10 resonators described by Eq. 1, where a slight difference in K_t results in different characteristic amplitudes for each resonator. We assume a difference in linear resonance frequency for adjacent resonators equal to one tenth of the resonator bandwidth. Panel (d) shows a cross section of the amplitude response at $f_d/f_0^1 = 1.2$, where f_0^1 is the linear resonance frequency of the slowest resonator. The phase response (not shown) also displays steep transitions similar to the amplitude, whose location can be determined with high accuracy [14]. The calculations thus reproduce the experimental findings in detail.

In conclusion, we have demonstrated an efficient way to operate and readout mechanical resonator arrays in dissipative environments. The center frequencies of the linear resonators can be spaced very closely as each resonator is marked by its characteristic drive amplitude at a fixed frequency, instead of the linear resonance frequency. As the exponential relation between required bandwidth and the number of resonators is circumvented, this technique may enable the construction of high-throughput resonant sensor arrays.

The authors acknowledge financial support from Koninklijke Philips NV (RWC-061-JR-05028) and from the Dutch organizations FOM and NWO (VICI).

[1] D. Karabacak, T. Kouh, C. C. Huang, and K. L. Ekinci, Appl. Phys. Lett. **88**, 19322 (2006).
[2] M. Li, H. X. Tang, and M. L. Roukes, Nat. Nanotechnol. **2**, 114 (2007).
[3] S. Dohn, O. Hansen, and A. Boisen, Appl. Phys. Lett. **88**, 264104 (2006).
[4] H. W. C. Postma, I. Kozinsky, A. Husain, and M. L.

Roukes, Appl. Phys. Lett. **86** (2005).
[5] J. Mertens, M. Alvarez, and J. Tamayo, Appl. Phys. Lett. **87** (2005).
[6] M. Yue, J. C. Stachowiak, H. Lin, R. Datar, R. Cote, and A. Majumdar, Nano Lett. **8**, 520 (2008).
[7] P. A. Truitt, J. B. Hertzberg, C. C. Huang, K. L. Ekinci, and K. C. Schwab, Nano Lett. **7** (2007).

- [8] C. A. Van Eysden and J. E. Sader, J. Appl. Phys. **100** (2006).
- [9] D. S. Greywall, Meas. Sci. Technol. **16**, 24732482 (2005).
- [10] J. G. E. Gardeniers, H. A. C. Tilmans, and C. C. G. Visser, J. Vac. Sci. Technol. A **14**, 2879 (1996).
- [11] K. Halbach, IEEE Trans. Nucl. Sci. **NS-30**, 3323 (1983).
- [12] A. N. Cleland and M. L. Roukes, J. Appl. Phys. **92**, 2758 (2002).
- [13] A. Bokaian, J. Sound Vib. **142**, 481 (1990).
- [14] D. S. Greywall, B. Yurke, P. A. Busch, A. N. Pargellis, and R. L. Willet, Phys. Rev. Lett. **72**, 2992 (1994).